

Ecole nationale des ponts et chaussées

Laboratoire d'Analyse des Matériaux et Identification

Jean-François Caron

ENPC composites expertise

The Four main themes are :

- **Civil Engineering** : construction, reinforcement and repair
- **Simulation** : design of composite structures
- **Testing facilities** : damage characterization (delamination, transverse cracking...)
- **Sports and leisure** : tennis rackets, skis and snowboards, archery bows manufacturing...

People activity



Dr Rui Pedro Carreira

Sports and leisure,
simulation



Pr. Dr Jean-François Caron

Composite group manager,
damage characterization,
multilayered models



Dr Olivier Baverel

Design of innovative
composite structures



Dr Gilles Foret

Construction
reinforcement and repair

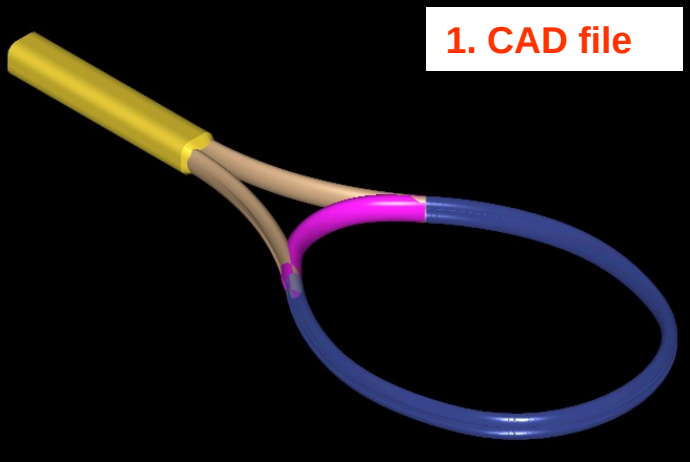
Sports and leisure applications

Enseignement des composites par l'objet sportif.

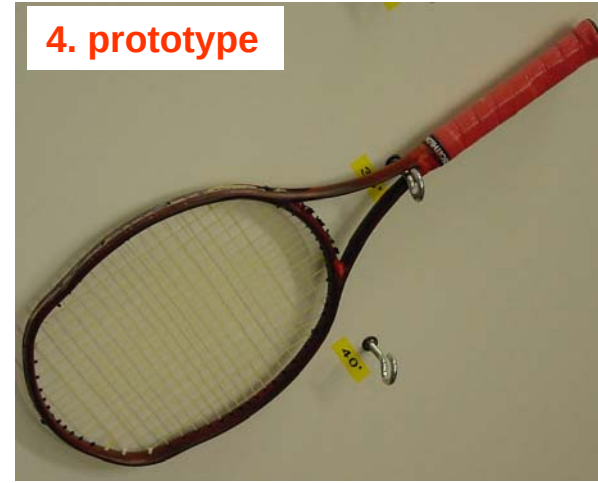
- ENPC, département Génie-Mécanique-Matériau
- Paris-Tech, (ENPC,ENSMP,ENSTA,ESPCI,...): Sem.Eurpéenne
- Ecole Polytechnique, Modex
- ESTIA, Bidard, Master sport de glisse,

Tennis racket elaboration

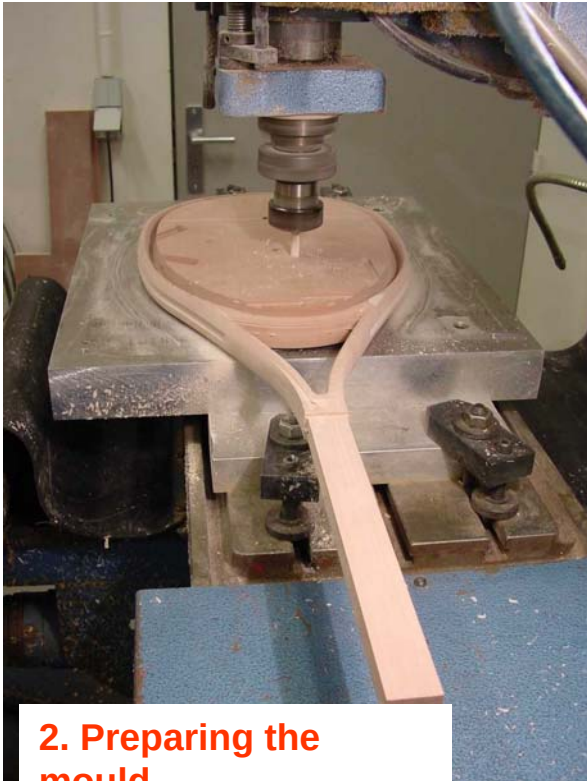
1. CAD file



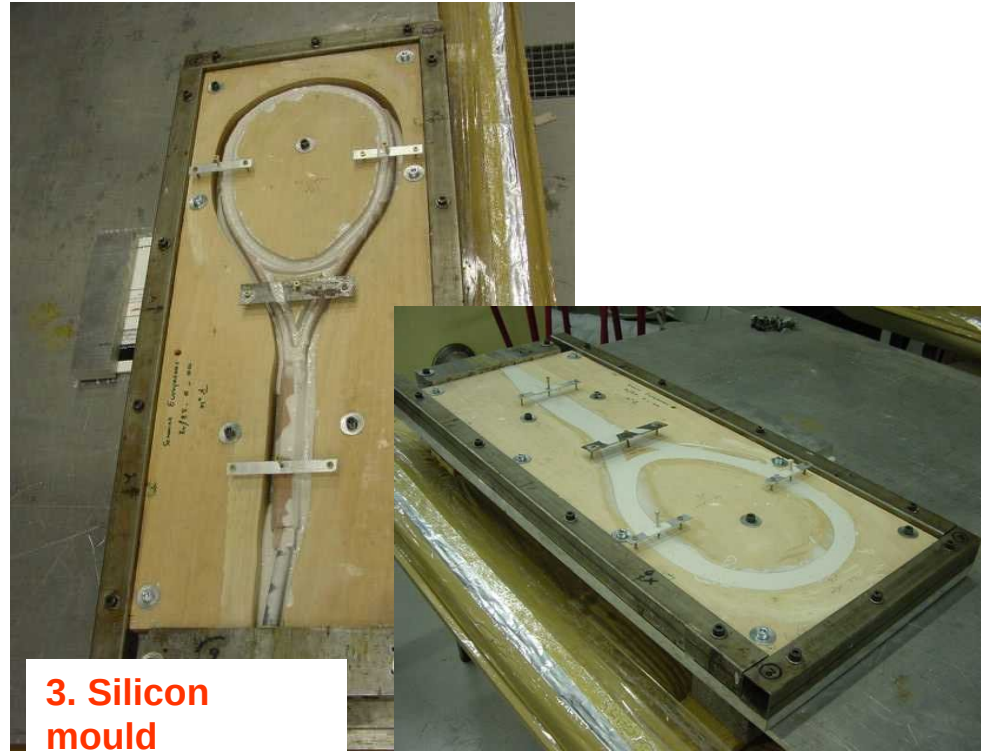
4. prototype



2. Preparing the
mould



3. Silicon
mould



Skis manufacturing

1. Skis lay-ups

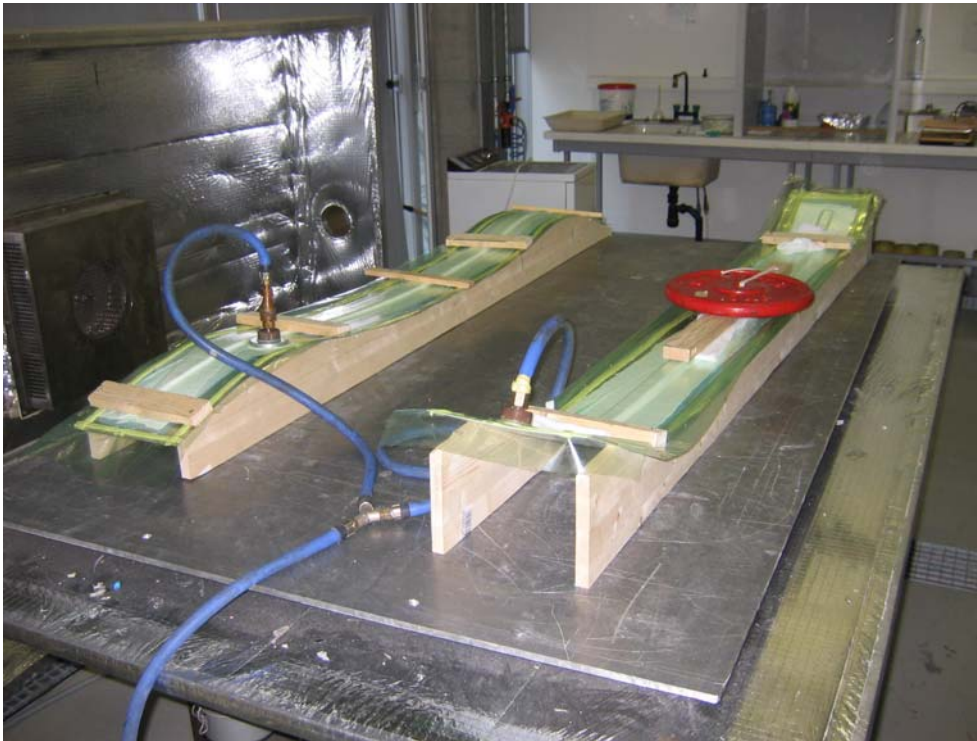


2. Curing



Long bow manufacturing

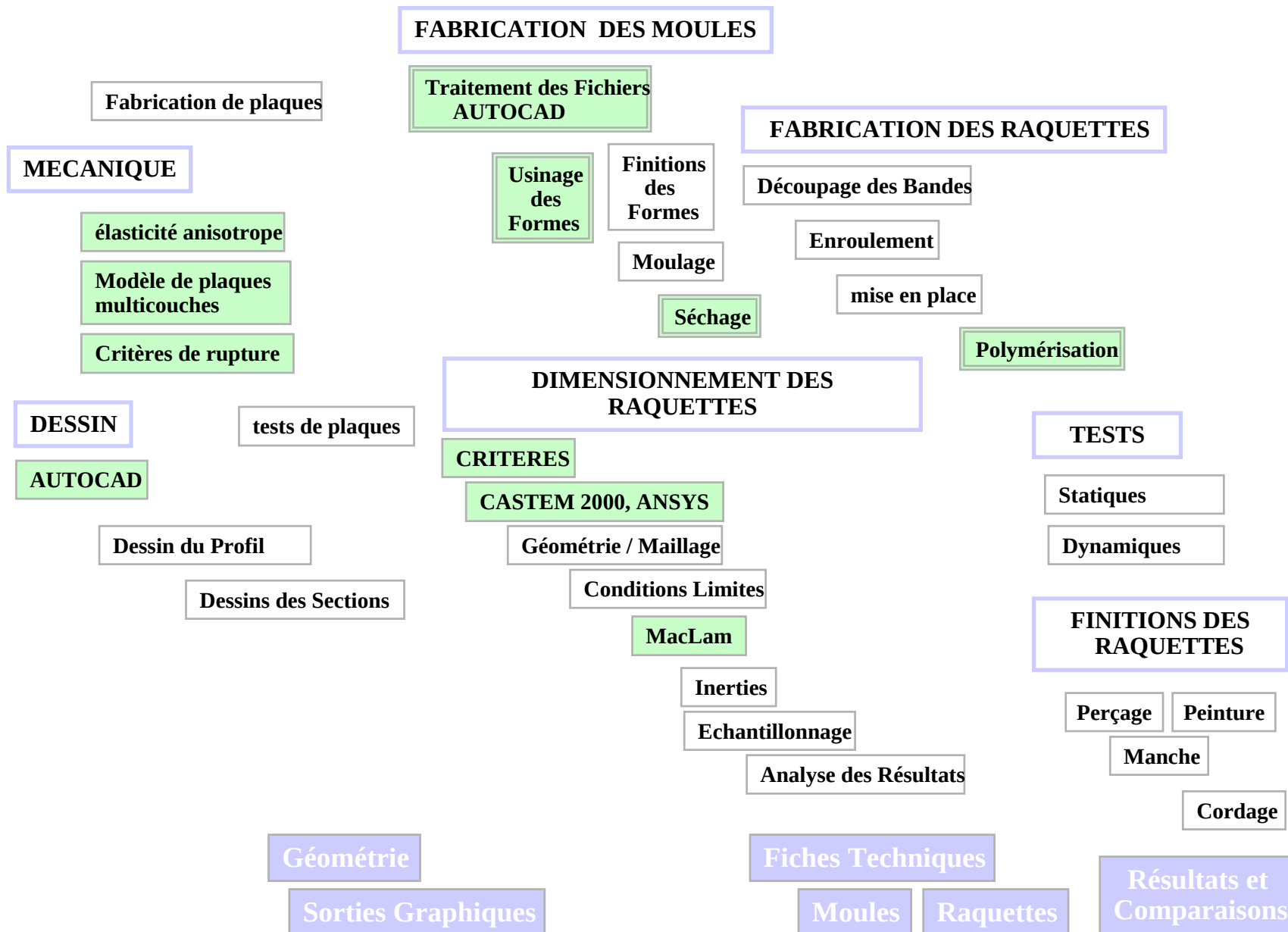
1. Bows lay-ups



2. Force draw curve characterization



EXPOSE INTRODUCTIF



Static Characteristics

- Weight



- Centre of gravity (balance)

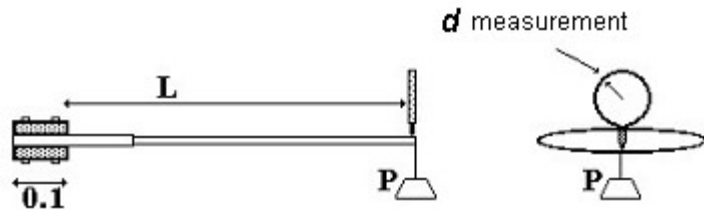


- Swing weight (weight distribution)

$$I = T^2 \frac{P(X_G - 0,1)}{4\pi 2} (kg.m^2)$$

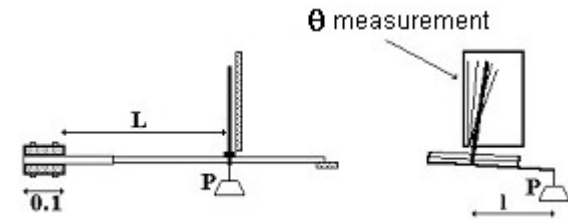


- Bending stiffness



$$K_{bending} = \frac{PL^3}{3d}$$

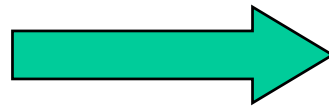
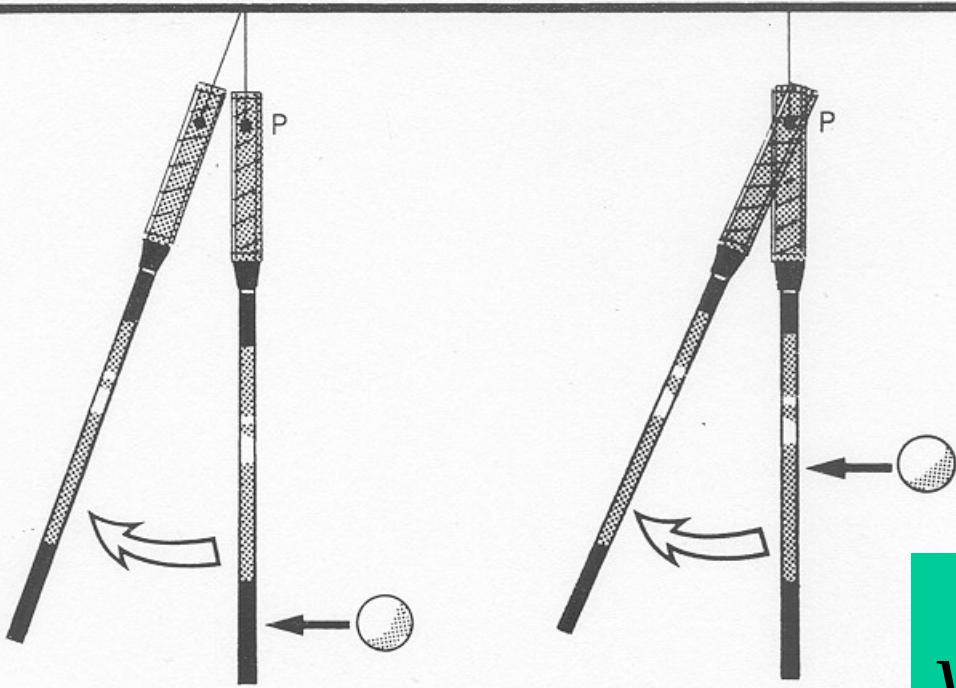
- Torsional stiffness



$$K_{torsion} = \frac{P.l.L}{\Theta}$$

Dynamic Characteristics

1. centre of percussion

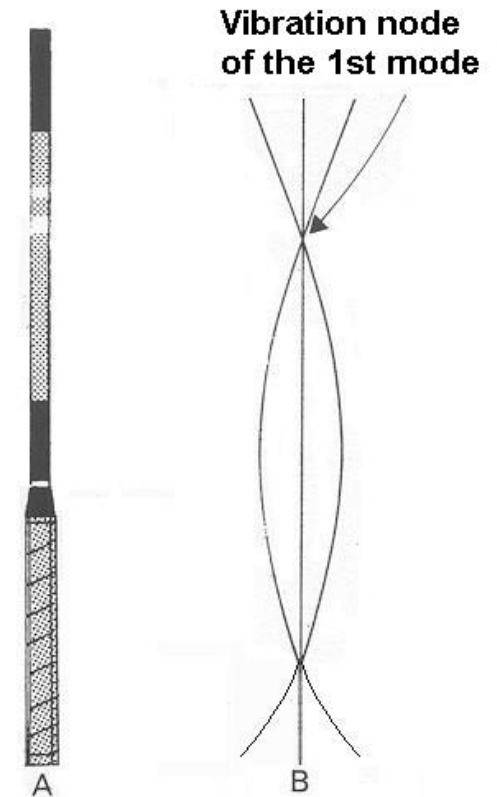


$$y_{C_P} = \frac{J_{xx} / P}{m(y_G - y_P)} + y_P$$

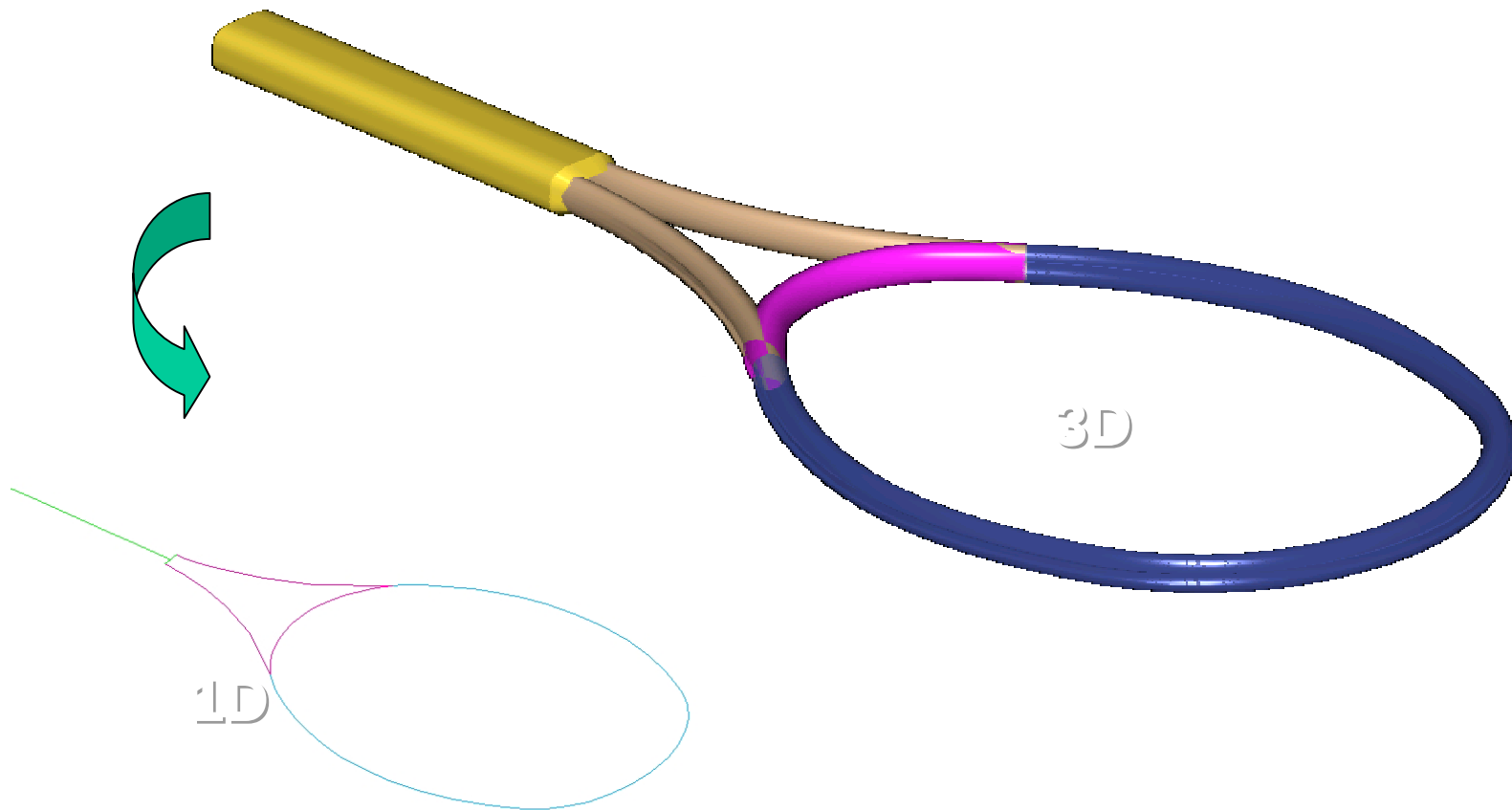
Vibratory analysis of the racquet as it is submitted at impact

2. What is the vibration node?

- 1st mode running to 150 Hz
- When the ball hits the racquet on the vibration node, the corresponding mode is not excited
- If the shot is offset, the player may suffer some “tennis elbow”
- Importance to make coincide node of vibration and geometrical center



I. Creation or importation of a geometrical model



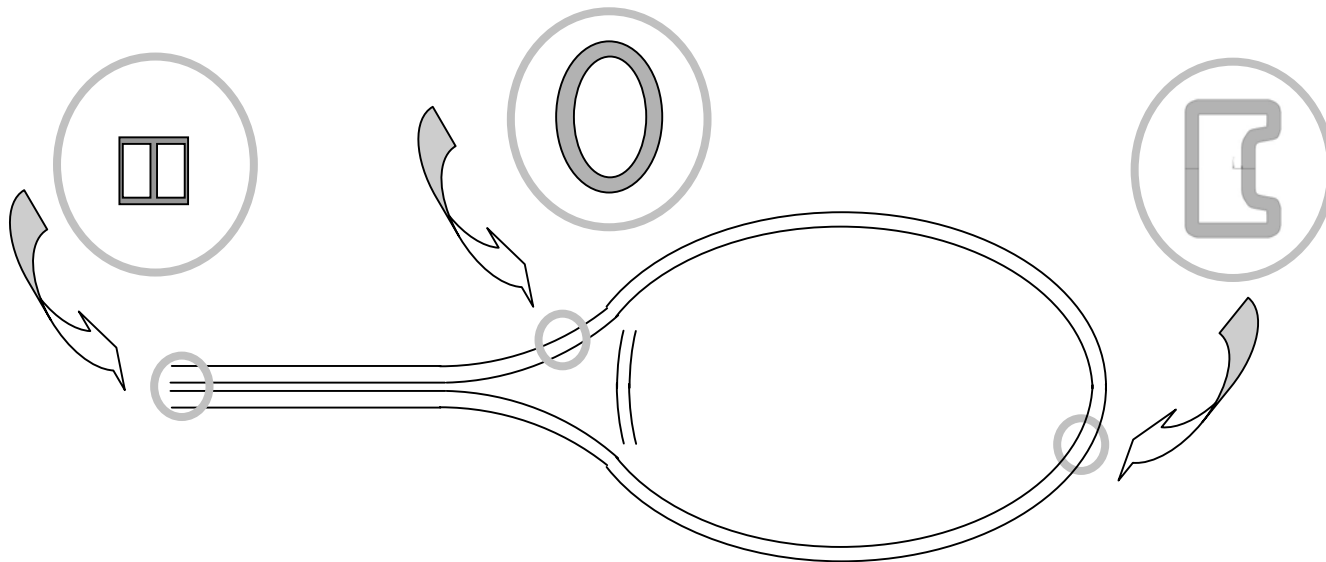
Description of a mechanical problem as a 1D FE model

- I. Creation or importation of a geometrical model
CAD model
- II. Choice and definition of the associated elements
beam, shell or volume
- III. Definition of the material properties
moduli, density
- IV. Meshing the model
- V. Loadings and displacements are applied
- VI. Performing the calculation
static linear, modal
- VII. Post processing the results
Deformed results, stresses

II. Choice and definition of the associated elements

III. Definition of the material properties

The FE model of the racquet is described by means of beams which characteristics (**geometry** and **material properties**) acting on stiffness are different according to whether it is the head, the throat or the handle.



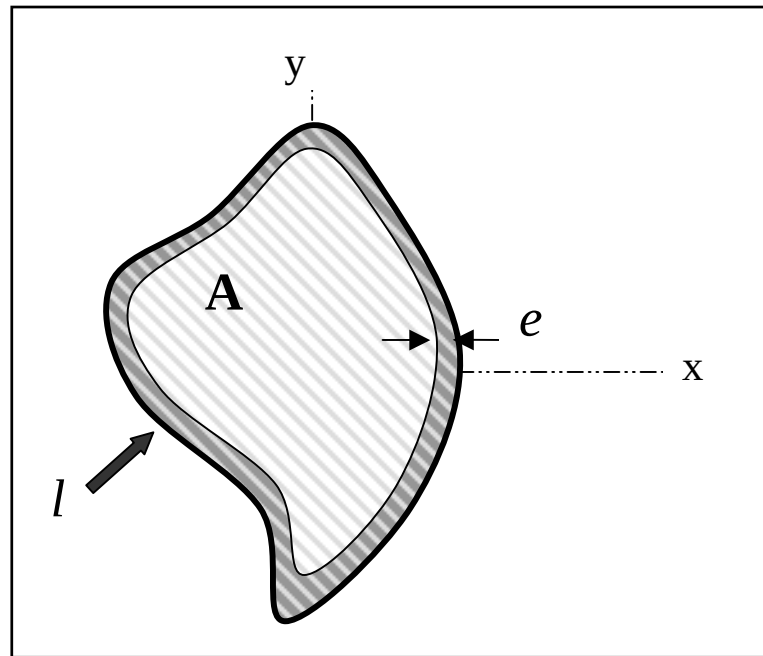
Calculation of moments of inertias for thin tube sections of unspecified form

It is thus necessary to calculate the moments of inertia for the various sections of the racquet (moments of inertia with respect each axis and the polar moment of inertia) depending on the outside geometry and the number of plies (thickness)

$$I_x = \int y^2 d\mu$$

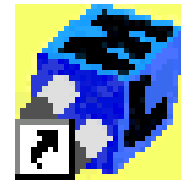
$$I_y = \int x^2 d\mu$$

$$I_z = \frac{4A^2 e}{l}$$



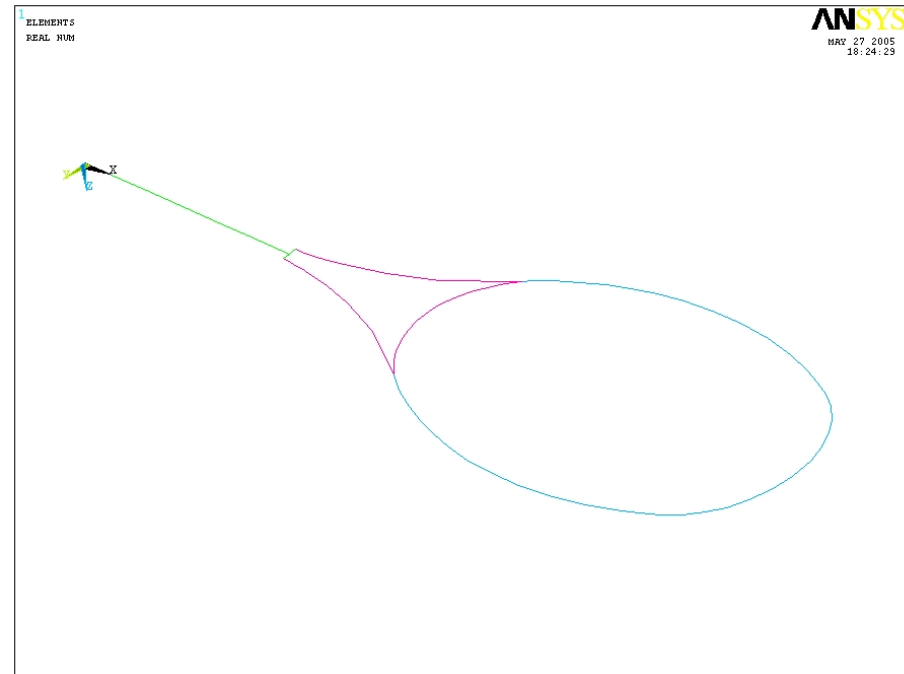
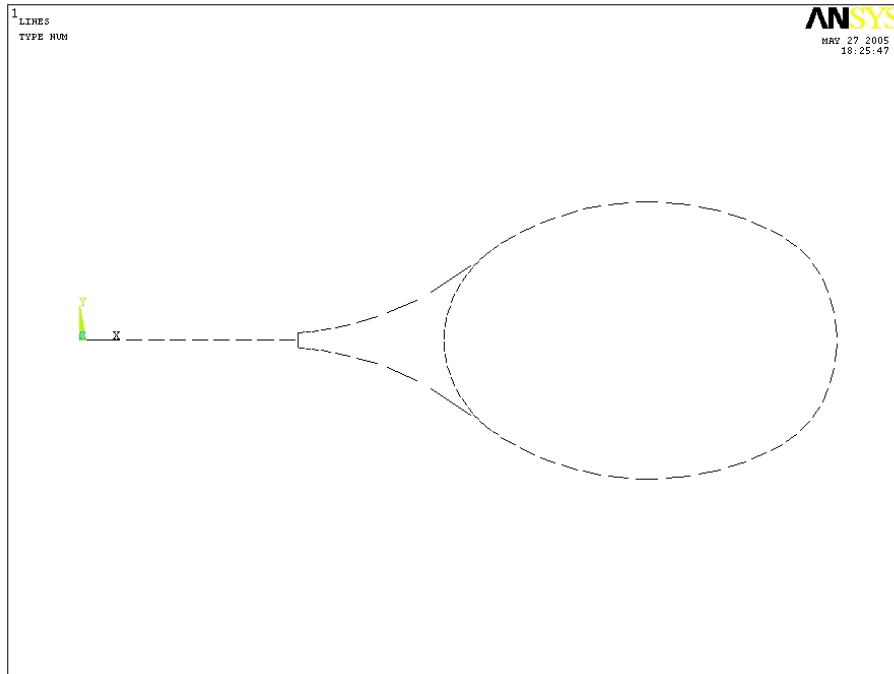
Calculation of the equivalent characteristics using Classical Lamination Theory

- Defining the composite ply (CFRP, GFRP):
 - Young's and shear moduli, Poisson's coefficient
 - ply thickness
 - density
- Creating the stacking sequence :
 - by combining different plies, their thicknesses and orientations
- Calculation of the equivalent properties (as needed to define the beam material property) :
 - E_{eq} (Young's modulus)
 - G_{eq} (shear modulus)

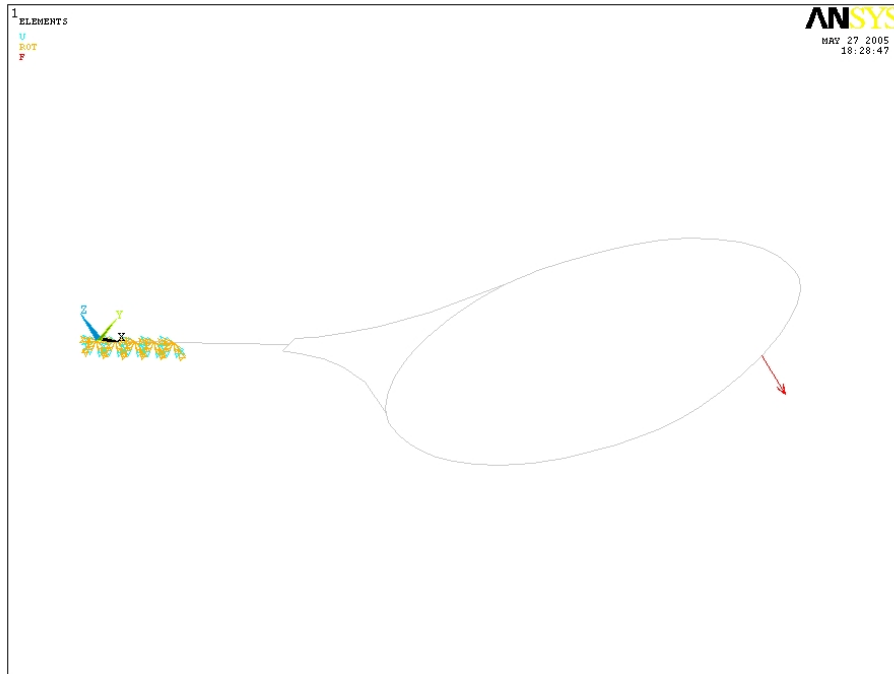


MAC LAM.Ink

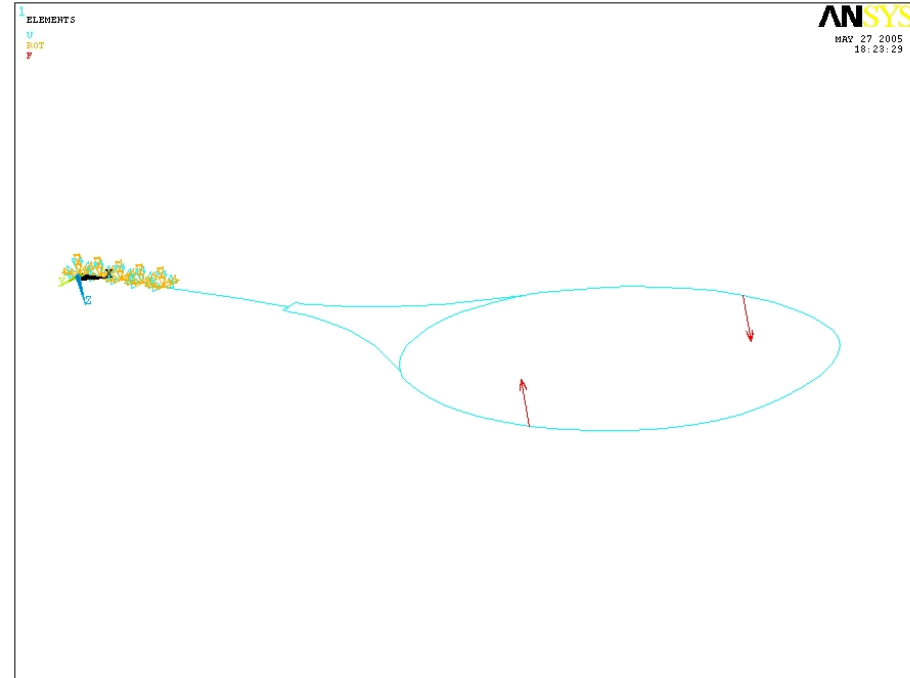
IV. Meshing the model



V. Loadings and displacements are applied



- Bending

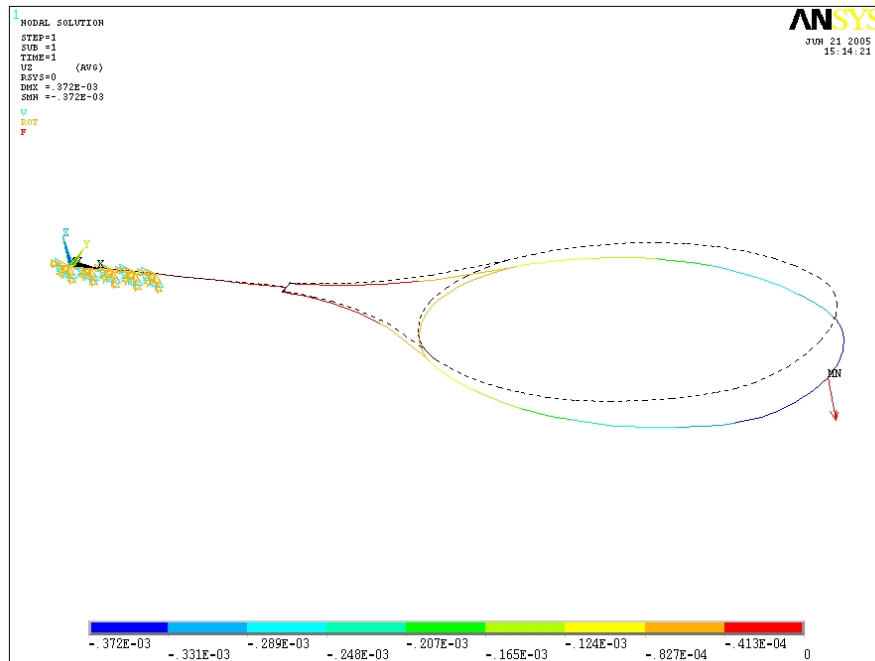


- Torsion

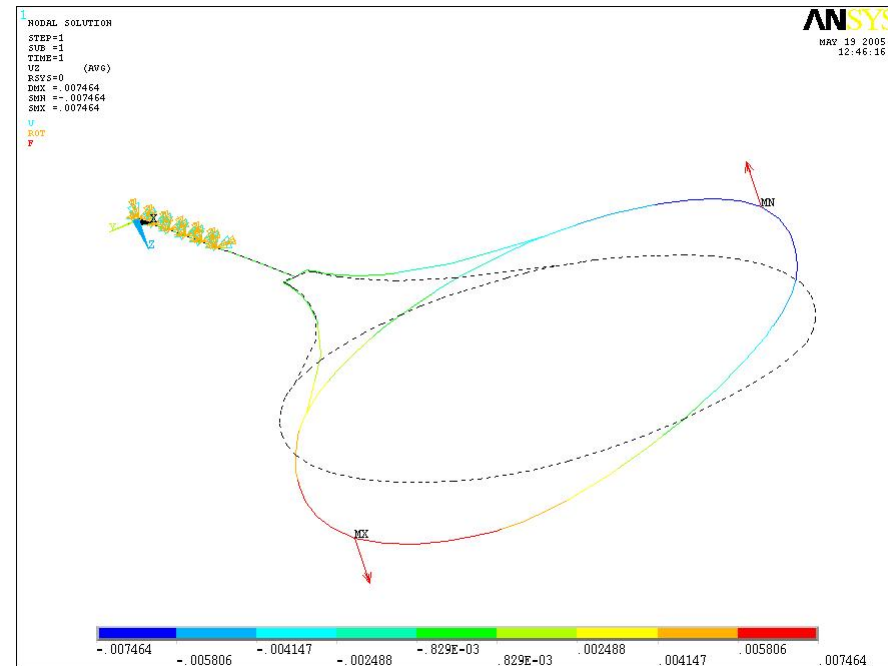
VI. Performing the calculation

VII. Post processing the results

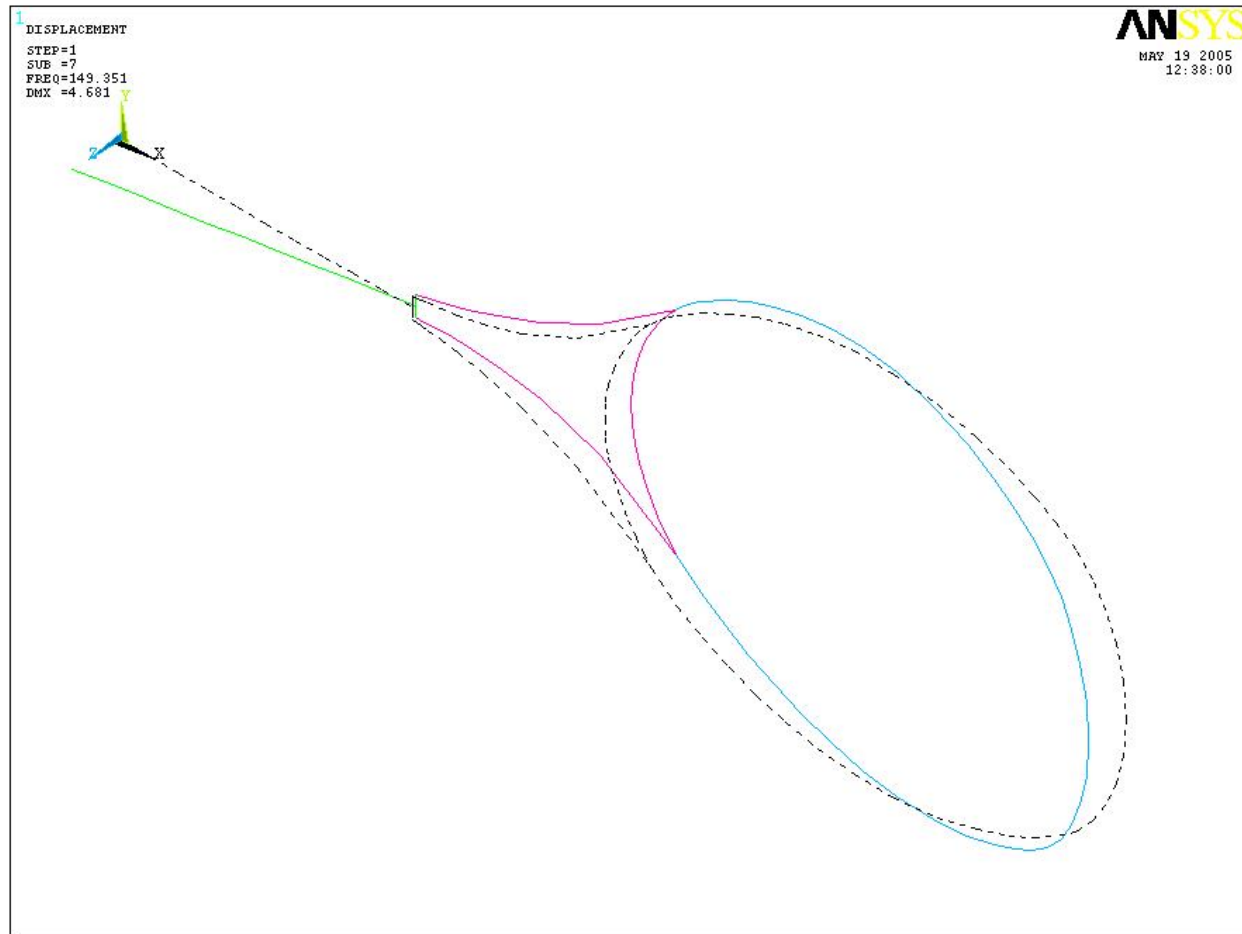
➤ displacement, angle, natural frequency



• Bending

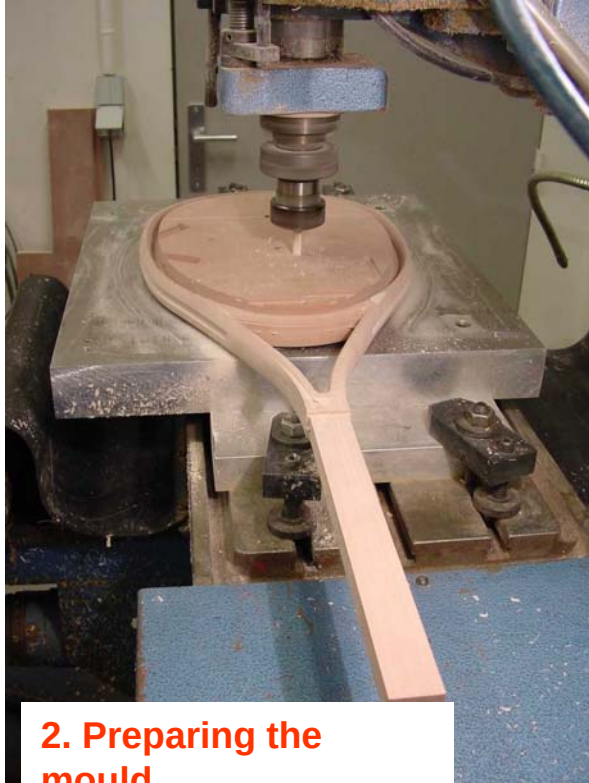


• Torsion



- Modal analysis

Tennis racket elaboration

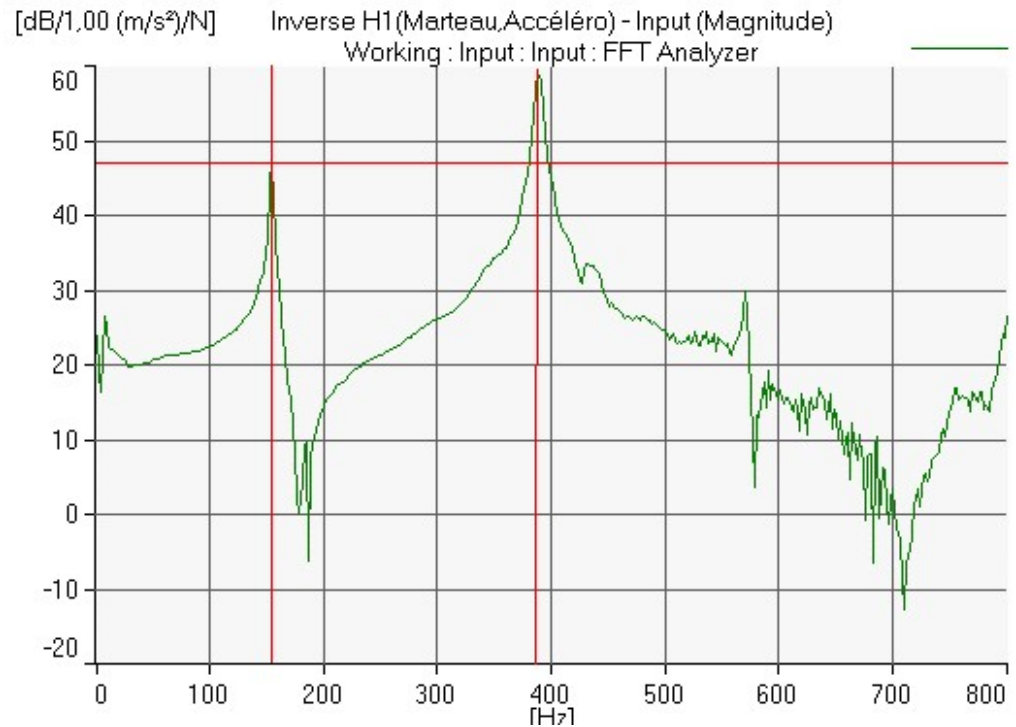
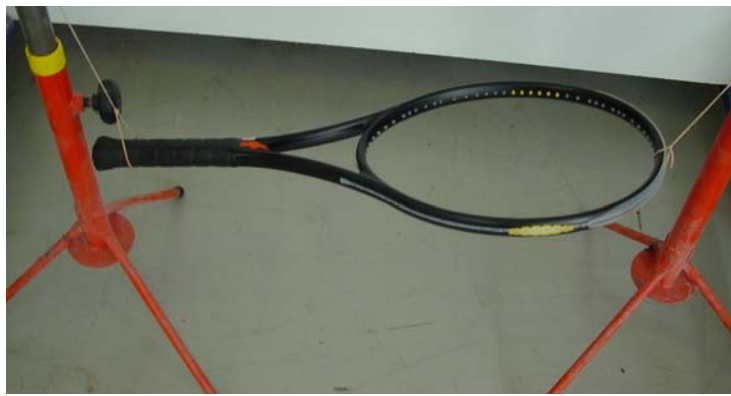


**2. Preparing the
mould**



**3. Silicon
mould**

Free boundary conditions measurements

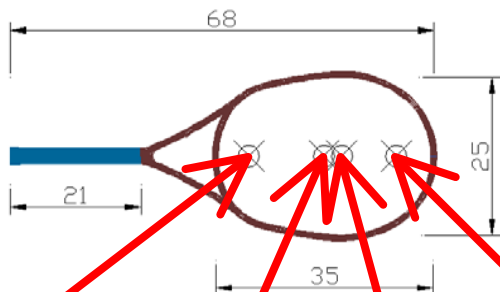


CONCEPTION D'UNE RAQUETTE DE TENNIS

CONCEPTION D'UNE RAQUETTE DE TENNIS

Molitorisz Peter
Vanderschelden Hugues
Dubié Loïc

Caractéristiques géométriques



Centre de masse

Centre de percussion

Centre du tamis

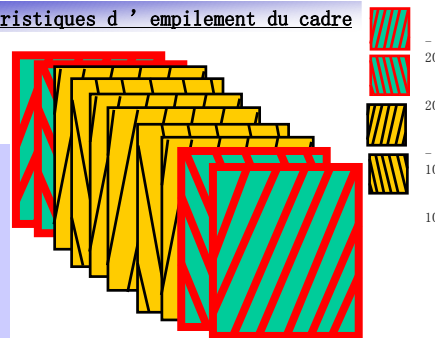
Nœud de vibration

Profil de la section du cadre



Caractéristiques d'empilement du cadre

Le cadre est empilé sur 10 couches (comme sur le dessin) et le manche est lui empilé sur 8 couches (sans les deux du milieu)



3ème manche

Tests

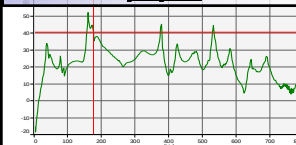
Statique :

Masse : 249 gr
Module de flexion : 146 N.m²
Module de torsion : 83 N.m²
Centre de masse : 38 cm
Centre de percussion : 50 cm

Dynamique :

Fréquence propre 1 : 36 Hz
Fréquence propre 2 : 178 Hz
Nœud de vibration : 61 cm

Visualisation des modes propres



4ème manche

Caractéristiques calculées avec Samcef

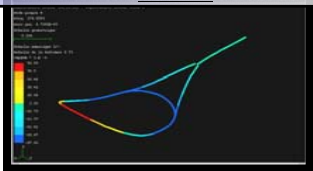
Statique :

Masse : 202 gr
Module de flexion : 135 N.m²
Module de torsion : 96 N.m²
Centre de masse : 38 cm
Centre de percussion : 50 cm

Dynamique :

Fréquence propre 1 : 34 Hz
Fréquence propre 2 : 178 Hz
Nœud de vibration : 62 cm

Visualisation de la déformée en flexion



2ème manche

La corrélation entre l'expérimentation et la théorie est très correcte aussi bien pour les résultats statiques que dynamiques.

La raquette finale

- Grand tamis (686 cm²) donc une bonne puissance.
- Equilibre de tête donc une bonne puissance et une bonne précision
- Le poids est correct et permet une bonne maniabilité

5ème manche

Conception d'une raquette de tennis

I - Dessin de la structure sous AutoCAD

Caractéristiques géométriques :

L'origine est prise au bout du manche



Longueur : 69,8 cm
Largeur : 26,4 cm
Surface tamis : 667 cm²
Masse de carbone : 211 g
Centre de gravité : 36,5 cm
Centre géométrique : 51,7 cm
Centre de percussion : 50,8 cm
Point pivot : 10 cm

II - Dimensionnement avec Castem

• Maillage



• Caractéristiques statiques

Module de flexion : 234 GPa
Module de torsion : 122 GPa

• Caractéristiques dynamiques

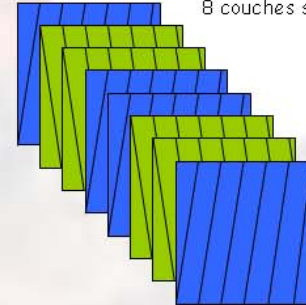
Modes propres de flexion :
- 1^{er} mode : 45 Hz < 50 Hz
- 2^{ème} mode : 228 Hz > 200 Hz
Nœud du 2^{ème} mode : 59,1 cm



C'est une raquette très rigide en flexion et très souple en torsion
pour joueur puissant et de bon niveau

III - Fabrication de la raquette

- Toute la raquette est réalisée avec un empilement de 8 couches symétrique équilibré : [15°, -15°, -15°, 15°]



Caractéristiques de l'empilement :

Épaisseur : 1,36 mm
Masse volumique : 1500 kg/m³
 E_{xx} : 80 GPa
 G_{xy} : 8 GPa

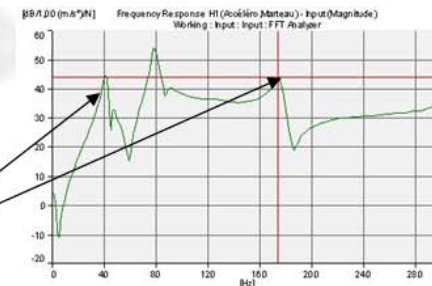
- Création de la chaussette (empilement, découpage)
- Cuison
- Démoulage et finition

IV - Tests

	Mesures	Erreur
Masse	238 g	12,7%
Module de flexion	219.5 GPa	5.3%
Module de torsion	105 GPa	13%
Centre de percussion	51.3 cm	1%

Les données mesurées
correspondent relativement bien
aux données théoriques

Flexion : 41Hz et 175 Hz



Ski and snowboard design



- 1. Introduction
- 2. Laboratory tests
- 3. FE model of a snowboard

- **1. Introduction**

- 2. Laboratory tests

- 3. FE model of a snowboard

« Skier » characteristics influent in ski or snowboard choice

- morphology (skier weight)
- skill level (beginner to expert)
- on-snow style (freeride / freestyle / freecarve)

...the speed increases from a "freestyle" approach towards a mode of "freeride" and especially one of "freecarve"...

The objective of the design : to achieve the adequacy between board / skier

Some ski and snowboard criteria

- Control
 - Accuracy of the trajectory
 - Forgiveness
- Manoeuvrability
 - Facility to change the direction, particularly sensible for freestyle
- Comfort
 - Absence of vibrations

Design steps

- Determine what criteria for a given use (according to style, technical and physical levels...)
- Taking process constraints into account
- By means of FEA using shell model:
 - height distribution
 - material choice
 - number of the plies
 - ply orientation

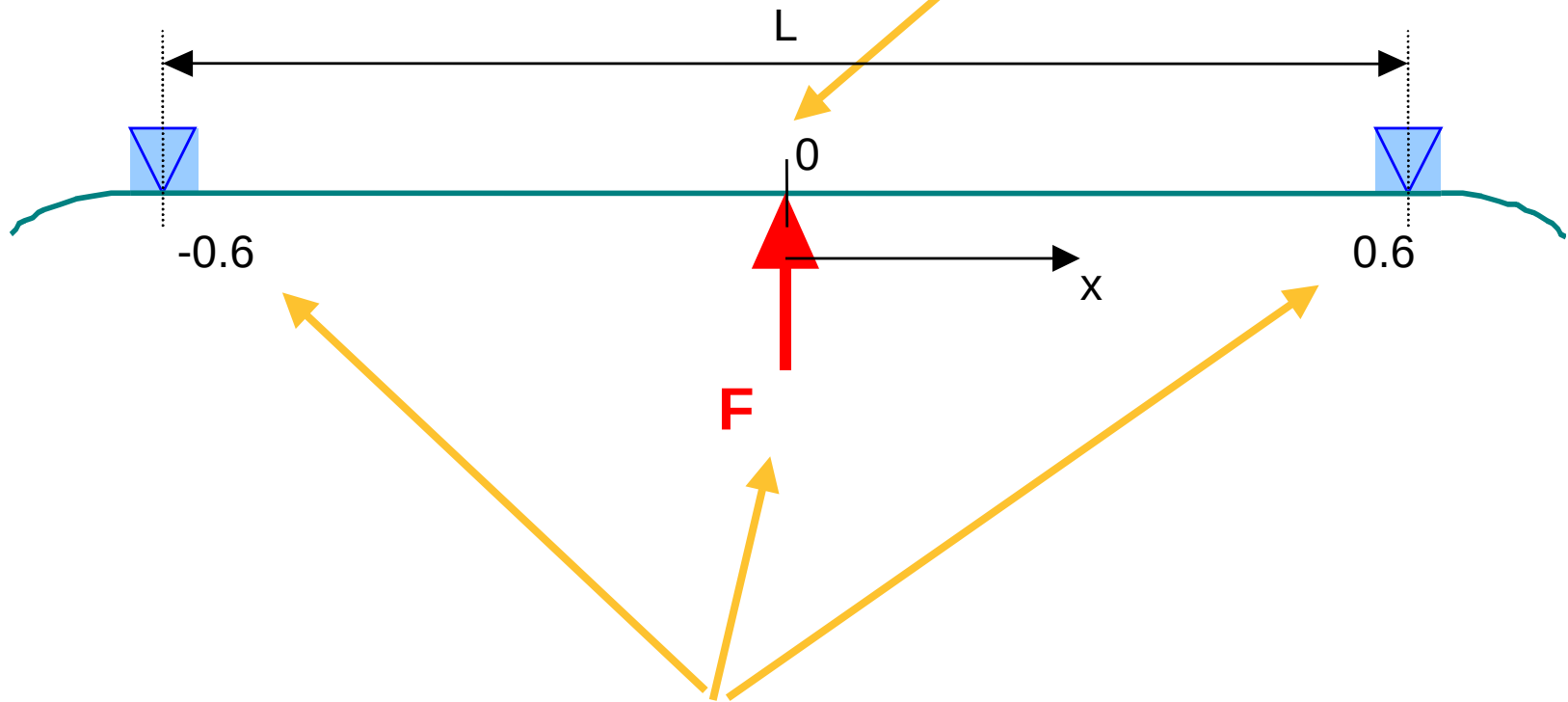
- 1. Introduction

- 2. Laboratory tests

- 3. FE model of a snowboard

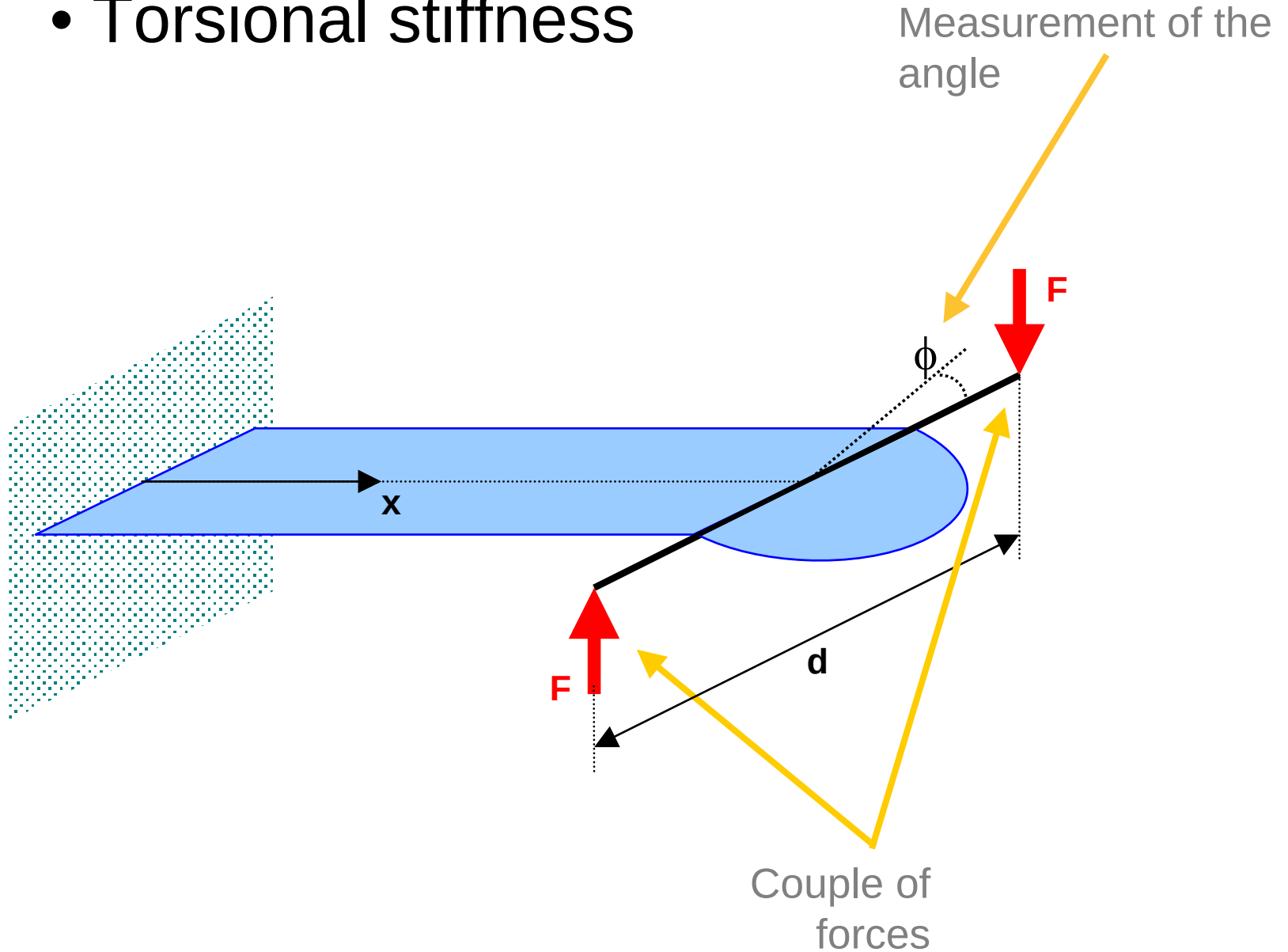
- Bending stiffness

Measurement of the displacement



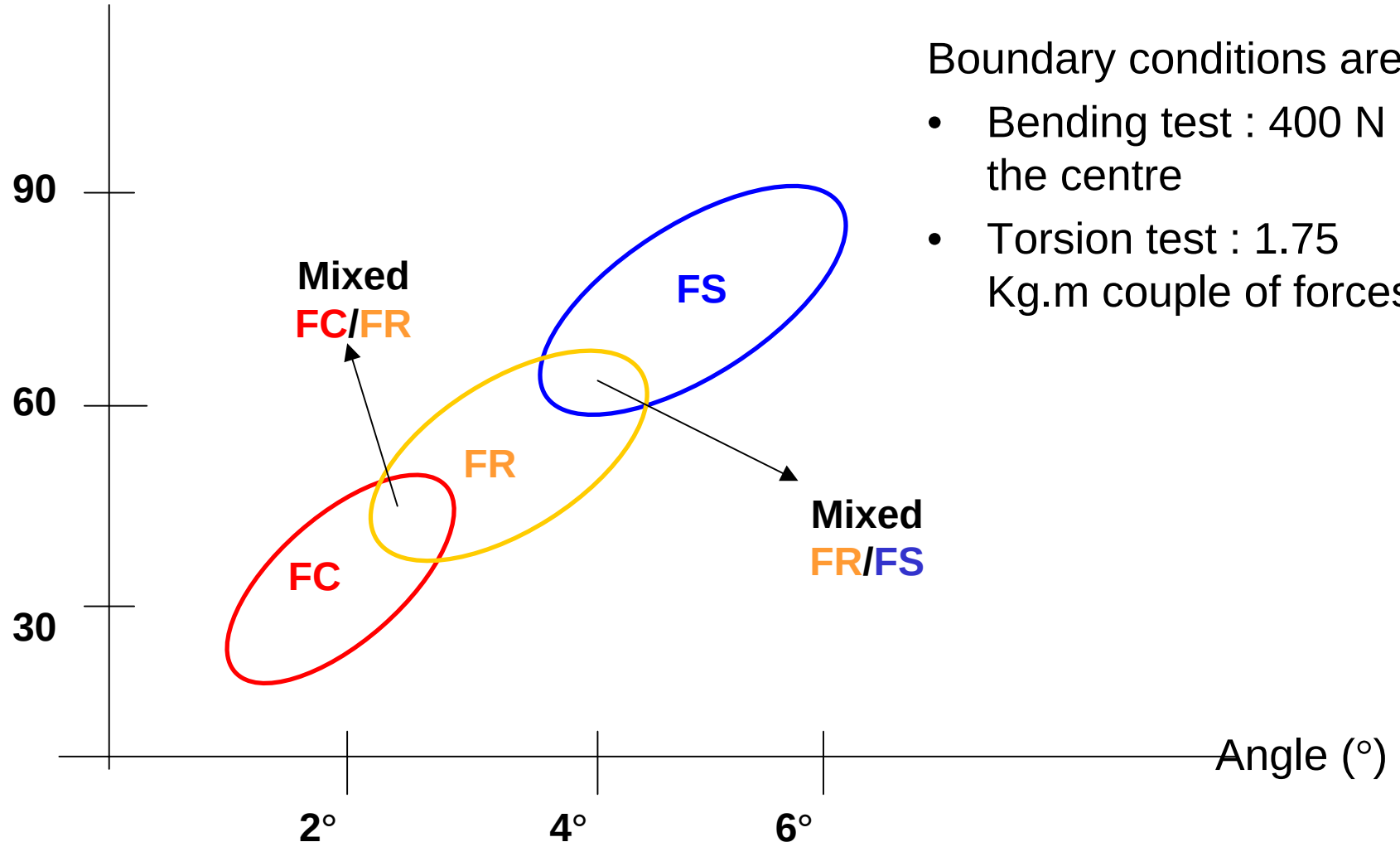
Three points bending

- Torsional stiffness



What characteristics will you choose according to your need?

Deflexion (mm)



Boundary conditions are :

- Bending test : 400 N at the centre
- Torsion test : 1.75 Kg.m couple of forces

- 1. Introduction
- 2. Laboratory tests
- 3. FE model of a snowboard

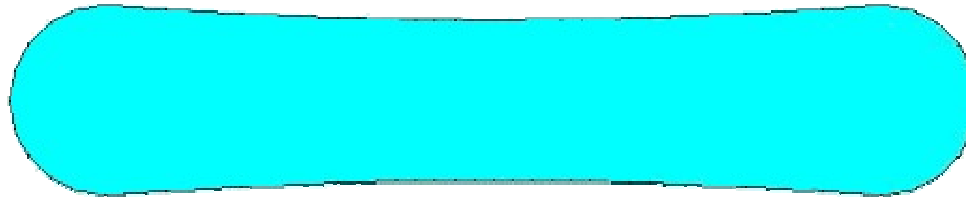
Description of a mechanical problem as a FE model

- I. Creation or importation of a geometrical model
CAD model
- II. Choice and definition of the associated elements
beam, shell or volume
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moduli, density
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- VI. Performing the calculation
static linear, modal
- VII. Post processing the results
Deformed results, stresses

I. Creation or importation of a geometrical model

1
ELEMENTS

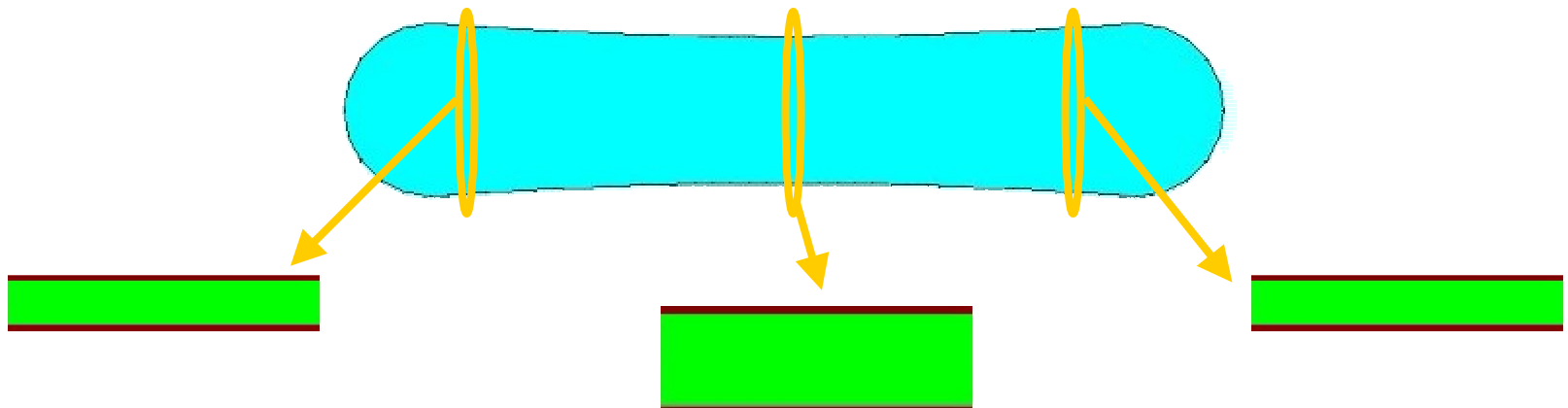
ANSYS
MAY 20 2005
14:26:05



II. Choice and definition of the associated elements

III. Definition of the material properties

The FE model of the snowboard is described by means of shells which characteristics (number of plies, associated thicknesses, ply orientations and material properties) are different according to the location on the ski or snow length.



Definition of a composite shell and creation of the stacking sequence by combining different plies and their thicknesses and orientations in **ANSYS**

Real Constant Set Number 1, for SHELL99

Element Type Reference No. 2

Number of layers (250 max) NL

Layer Symmetry Key LSYM

First layer for output LP1

Second layer for output LP2

Elastic foundation stiffness EFS

Added mass/unit area ADMSUA

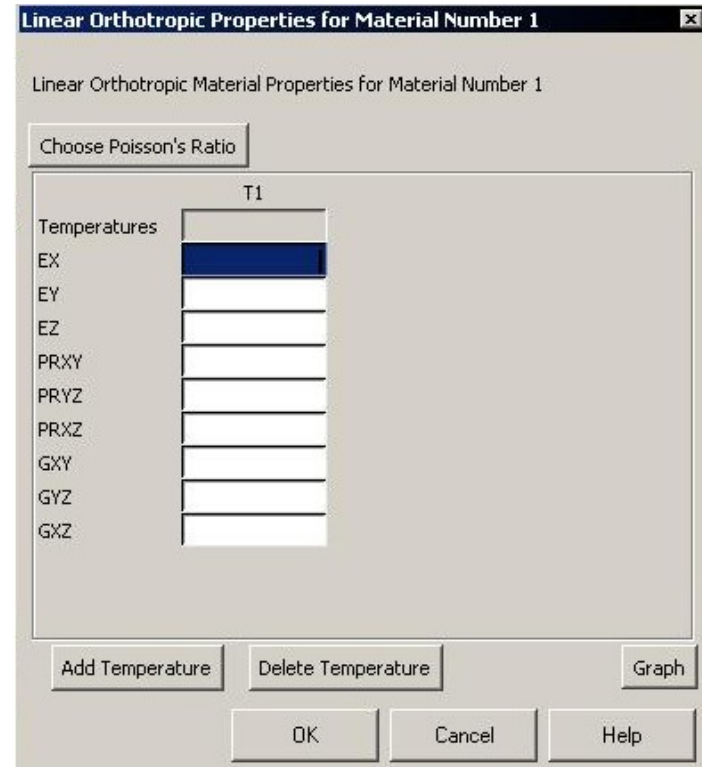
Real Constant Set Number 2, for SHELL99

Mat no., X-axis rotation, layer thk	MAT	THETA	TK
Layer number 1	1	0	0.17
Layer number 2	1	90	0.17
Layer number 3	1	90	0.17
Layer number 4	1	0	0.17

Definition of the material properties of an orthotropic material in **ANSYS**

Defining the composite ply :

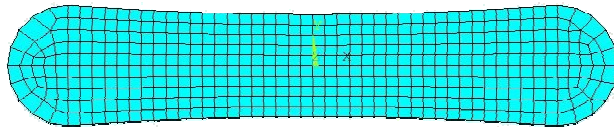
- Young's and shear moduli, Poisson's coefficient
- density



IV. Meshing the model

1
ELEMENTS
REAL NUM

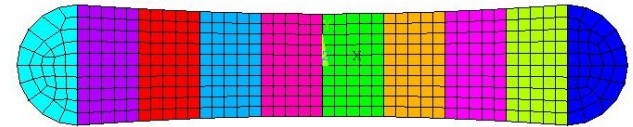
ANSYS
MAY 20 2005
14:26:05



1
ELEMENTS
REAL NUM

1
ELEMENTS
REAL NUM

ANSYS
MAY 20 2005
14:25:28



ANSYS
MAY 20 2005
14:36:56

Different stacking
sequences groups

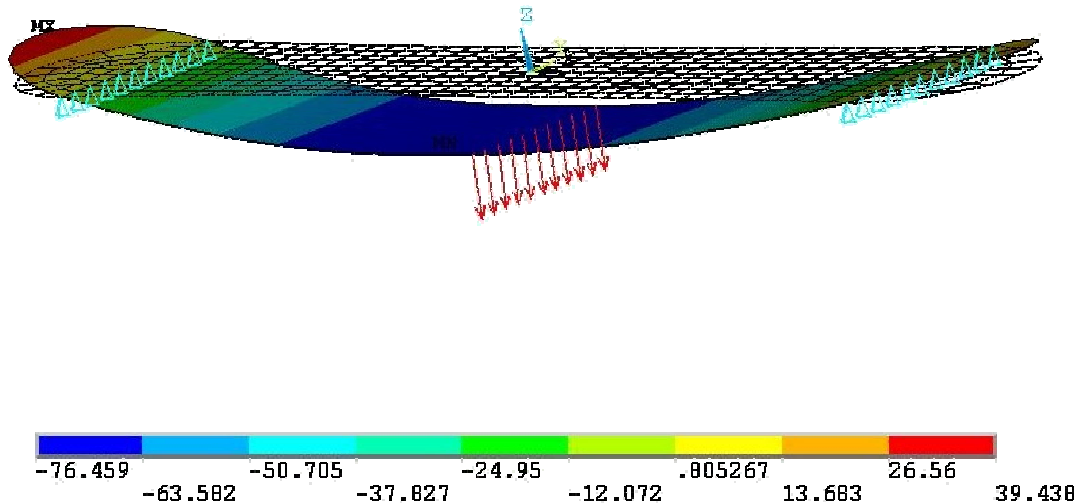


- V. Loadings and displacements are applied
- VI. Performing the calculation
- VII. Post processing the results

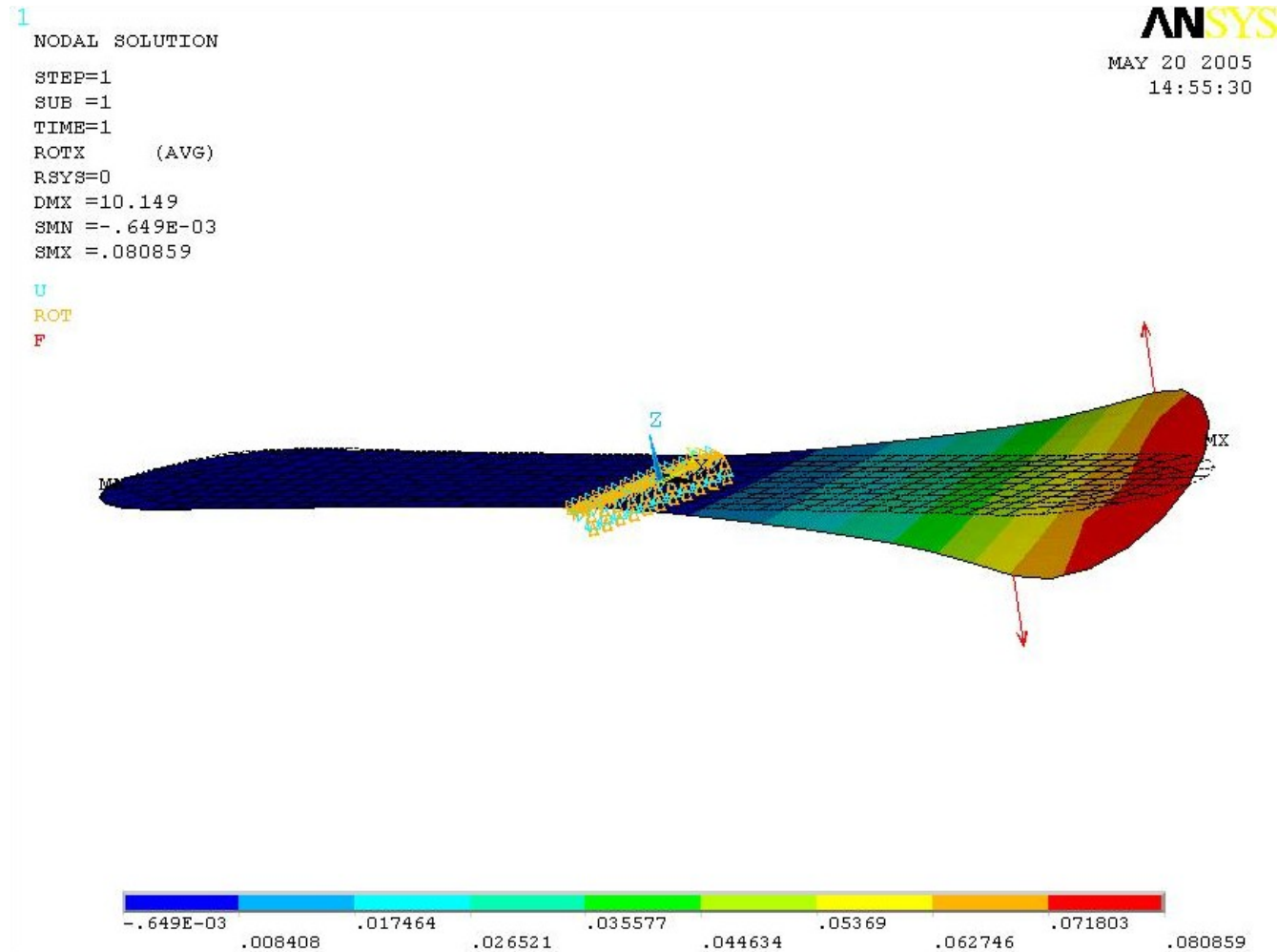
- Bending

```
1
NODAL SOLUTION
STEP=1
SUB =1
TIME=1
UZ      (AVG)
RSYS=0
DMX  =76.565
SMN  =-76.459
SMX  =39.438
U
F
```

ANSYS
MAY 20 2005
15:04:25



• Torsion



• Natural frequencies

1
DISPLACEMENT
STEP=1
SUB =7
FREQ=17.605
DMX =92.881



Video Clip

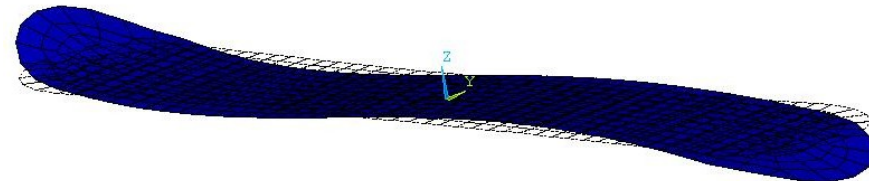
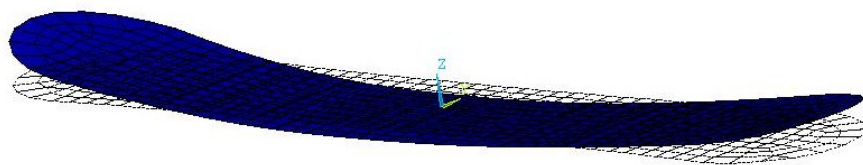
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MAY 20 2005
15:49:27

1
DISPLACEMENT
STEP=1
SUB =8
FREQ=37.163
DMX =130.961



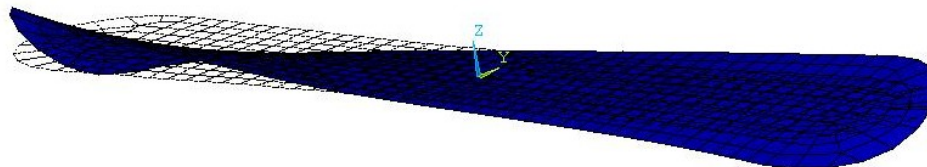
Video Clip

ANSYS
MAY 20 2005
15:50:40



1
DISPLACEMENT
STEP=1
SUB =9
FREQ=54.407
DMX =103.078

ANSYS
MAY 20 2005
15:51:35



Video Clip

Thank you very much